

Name KEY

Show your work on all problems, and leave your solutions in the simplest form possible. Perform the indicated operations. Simplify when possible.

$$\frac{a-5b}{a+b} - \frac{a+7b}{a+b}$$

$$= \frac{a-5b-(a+7b)}{a+b}$$

$$= \frac{-12b}{a+b}$$

$$\frac{4xy}{x^2-y^2} + \frac{x-y}{x+y}$$

$x^2 - y^2 = (x-y)(x+y)$	Rem 1
$x + y = x + y$	(x-y)

$$\text{LCM} = (x-y)(x+y)$$

$$= \frac{4xy(1) + (x-y)(x-y)}{(x-y)(x+y)}$$

$$= \frac{4xy + x^2 - 2xy + y^2}{(x-y)(x+y)}$$

$$= \frac{x^2 + 2xy + y^2}{(x-y)(x+y)} = \frac{(x+y)^2}{(x-y)(x+y)}$$

$$= \boxed{\frac{x+y}{x-y}}$$

$$N \left\{ \frac{x}{x-2} + \frac{x}{x-1} \right.$$

$$D \left. \left\{ \frac{3}{x^2-1} + \frac{x}{x-1} \right. \right.$$

$x-2 = x-2$	Rem x-1
$x-1 = x-1$	x-2

$$\text{LCM} = (x-1)(x-2)$$

$x^2-1 = (x-1)(x+1)$	Rem 1
$x-1 = x-1$	x+1

$$\text{LCM} = (x-1)(x+1)$$

$$N = \frac{x(x-1) + x(x-2)}{(x-1)(x-2)}$$

$$= \frac{x^2 - x + x^2 - 2x}{(x-1)(x-2)}$$

$$= \frac{2x^2 - 3x}{(x-1)(x-2)} = \boxed{\frac{x(2x-3)}{(x-1)(x-2)}}$$

$$D = \frac{3(1) + x(x+1)}{(x-1)(x+1)} = \boxed{\frac{3+x^2+x}{(x-1)(x+1)}}$$

$$N \div D = \frac{x(2x-3)}{(x-1)(x-2)} \cdot \frac{(x-1)(x+1)}{x^2+x+3}$$

$$= \boxed{\frac{x(2x-3)(x+1)}{(x-2)(x^2+x+3)}}$$